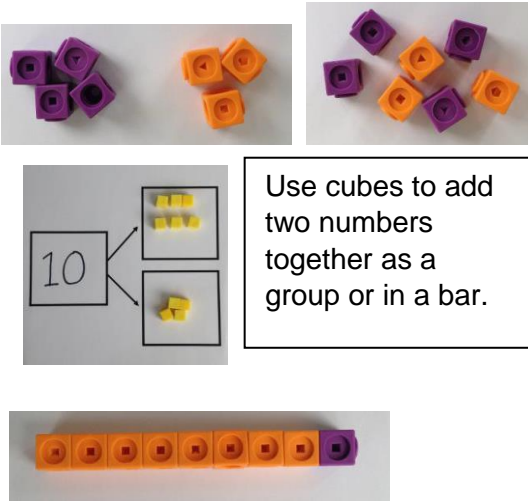
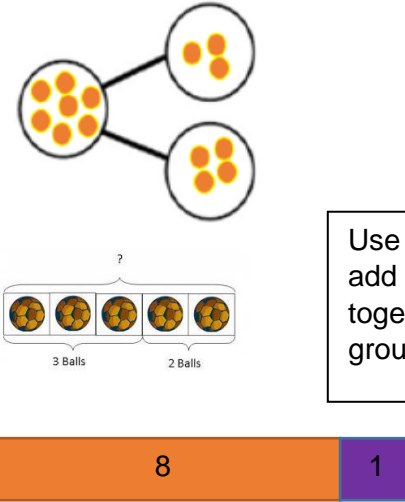
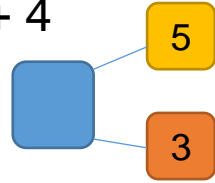
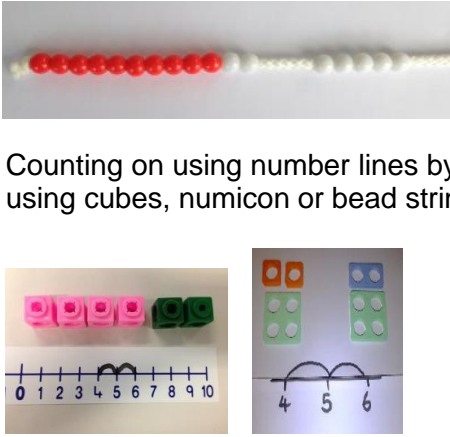
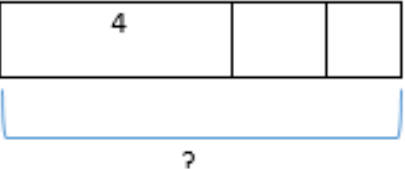
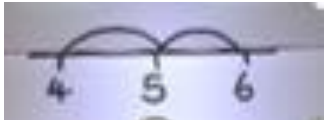
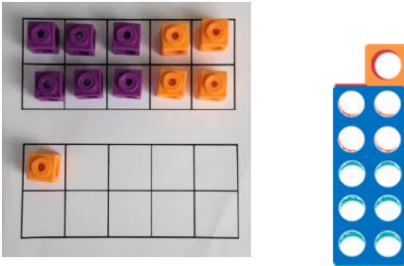
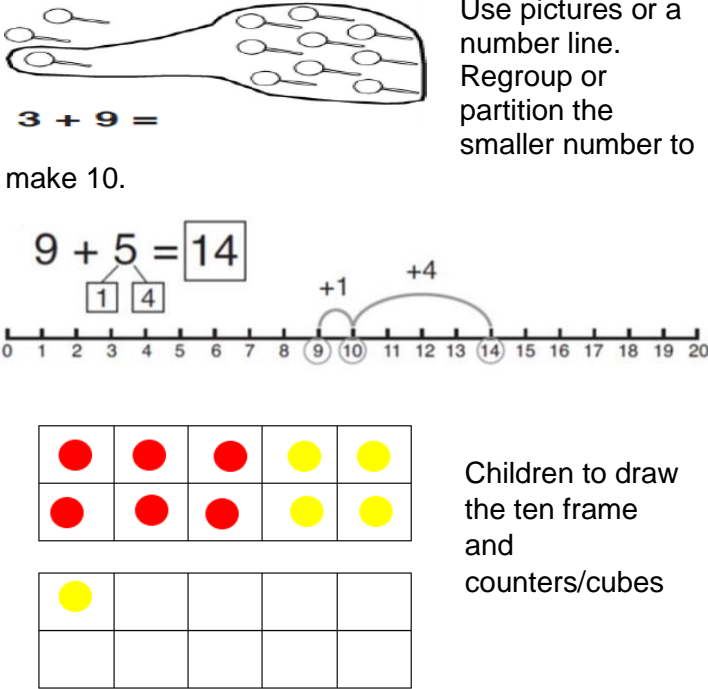

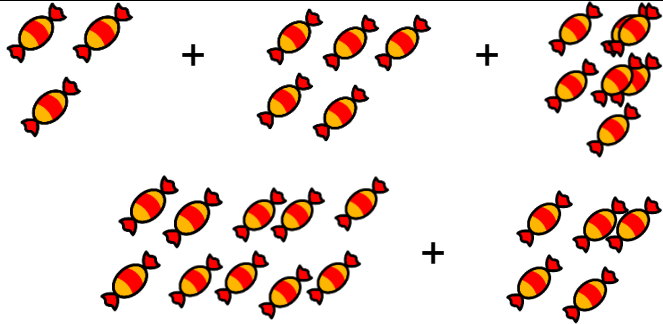


Progression in Calculations

Addition

Key vocabulary – sum, total, parts and wholes, plus, add, altogether, more than, 'is equal to', 'is the same as'

(Year group) Objective and Strategies	Concrete	Pictorial	Abstract
<p>(Year 1) Combining two parts to make a whole: part-whole model</p>	 <p>Use cubes to add two numbers together as a group or in a bar.</p> <p>Use a variety of resources</p>	 <p>Use pictures to add two numbers together as a group or in a bar.</p>	<p>$4 + 3 = 7$</p> <p>$10 = 6 + 4$</p>  <p>Use the part-part whole diagram as shown above to move into the abstract.</p>
<p>(Year 1) Starting at the bigger number and counting on</p>	 <p>Counting on using number lines by using cubes, numicon or bead strings.</p>	<p>A bar model which encourages the children to count on.</p> 	<p>The abstract number line:</p> <p>What is 2 more than 4?</p> <p>What is the sum of 4 and 4?</p> <p>What's the total of 4 and 2?</p> <p>$4 + 2$</p>  <p>This can progress all the way</p>

			to counting on using 2 digit numbers and gear. (year2)
<p>(Year 1)</p> <p>Regrouping to make 10 by using ten frames and counters/cubes or using numicon.</p>	<p>$6 + 5 = 11$</p> <p>Start with the bigger number and use the smaller number to make 10.</p> 	 <p>Use pictures or a number line. Regroup or partition the smaller number to make 10.</p> <p>Children to draw the ten frame and counters/cubes</p>	<p>$7 + 4 = 11$</p> <p>If I am at seven, how many more do I need to make 10. How many more do I add on now?</p> <p>Children to develop an understanding of equality e.g.</p> <p>$6 + \square = 11$ and</p> <p>$6 + 5 = 5 + \square$</p> <p>$6 + 5 = \square + 4$</p>
<p>(Year 2)</p> <p>Adding three single digits</p>	<p>$4 + 7 + 6 = 17$</p> <p>Put 4 and 6 together to make 10. Add on 7.</p>  <p>Following on from making 10, make 10 with 2 of the digits (if possible) then add on the third digit.</p>	 <p>Add together three groups of objects. Draw a picture to recombine the groups to make 10.</p>	<p>$4 + 7 + 6 = 10 + 7 = 17$</p> <p>Combine the two numbers that make 10 and then add on the remainder.</p>

(Year 2)
2-digit + 1/2
digit, column
method- no
regrouping
and counting

On. (See Year1 for
concrete and pictorial)

TO + O using base 10. Continue to
develop understanding of partitioning
and place value

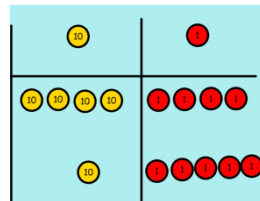
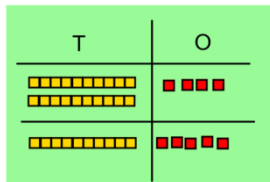
$$41 + 8$$



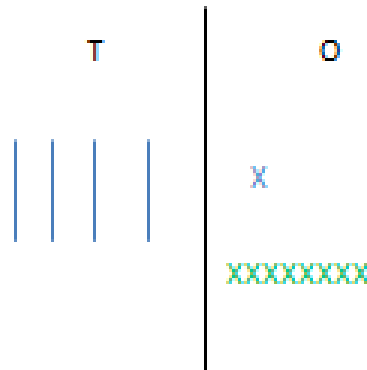
Progress onto TO + TO using base 10

$$24 + 15 =$$

Add together the ones first then add the
tens. Use the Base 10 blocks first before
moving onto place value counters.

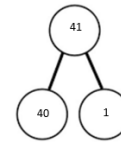


Children to represent the concrete using a particular
symbol, e.g. lines for 10s and dots/crosses for ones.



See Year 1 for bar model image.

$$41 + 8$$



$$1 + 8 = 9$$

$$40 + 9 = 49$$

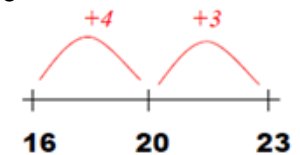
	4	1
+		8
<hr/>		
	4	9

Calculations

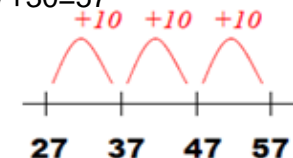
$$21 + 42 =$$

$$\begin{array}{r} 21 \\ + 42 \\ \hline \end{array}$$

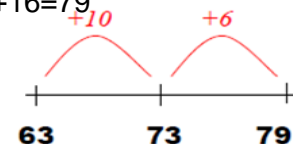
$$16 + 7 = 23$$



$$27 + 30 = 57$$









$$63 + 16 = 79$$

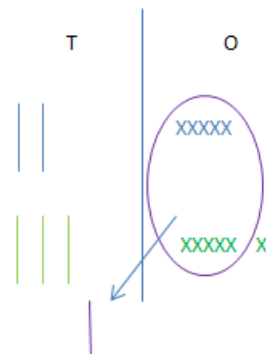


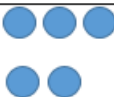
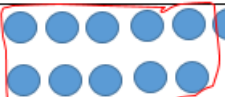
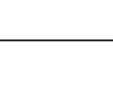
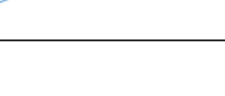
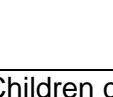

(Year 2)
Column
method-
regrouping

TO + TO using base 10. Continue to develop understanding of partitioning and place value and use this to support addition. Begin with no exchanging. $36 + 25$

	Tens	Ones
+		
		
=		

This could be done one of two ways.



Tens	Ones
	
	
	

Looking for ways to make 10

$$\begin{array}{r}
 36 + 25 = \\
 \begin{array}{cc}
 1 & 5 \\
 \diagup & \diagdown \\
 36 & 25
 \end{array}
 \end{array}$$

$30 + 20 = 50$
 $5 + 5 = 10$
 $50 + 10 + 1 = 61$

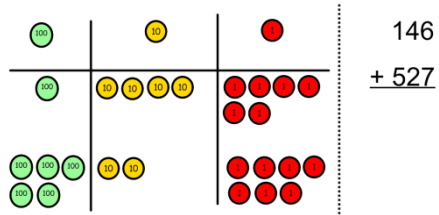
(Year 3 and
beyond)
Column
method-
regrouping

Use Base 10 or place value counters. Make both numbers on a place value grid.

Children can draw a pictorial representation of the columns and place value counters to further support their learning and understanding.

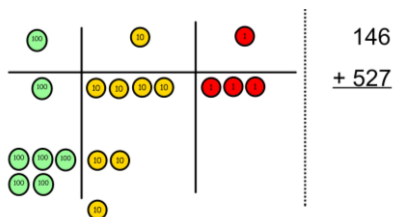
Start by partitioning the numbers before moving on to clearly show the exchange below the addition.

$$\begin{array}{r}
 20 + 5 \\
 40 + 8 \\
 \hline
 60 + 13 = 73
 \end{array}$$



$$\begin{array}{r} 146 \\ + 527 \\ \hline \end{array}$$

Add up the ones and exchange 10 ones for one 10.

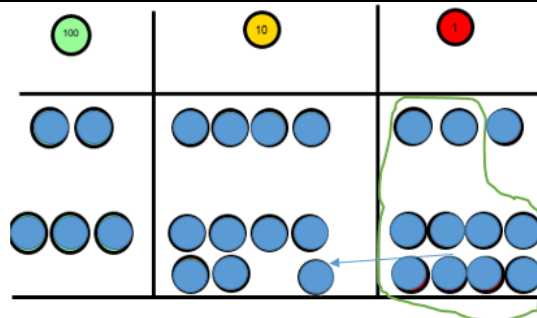


$$\begin{array}{r} 146 \\ + 527 \\ \hline \end{array}$$

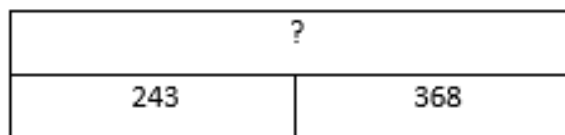
Add up the rest of the columns, exchanging the 10 counters from one column for the next place value column until every column has been added.

This can also be done with Base 10 to help children clearly see that 10 ones equal 1 ten and 10 tens equal 100.

As children move on to decimals, money and decimal place value counters can be used to support learning.



If the children are completing a word problem, draw a bar model to represent what it's asking them to do.



536

+ 85

621

11

As the children move on, introduce decimals with the same number of decimal places and different. Money can be used here.

72.8

+ 54.6

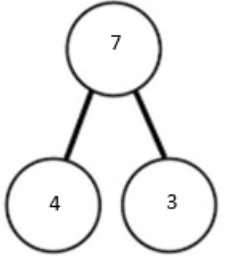
127.4

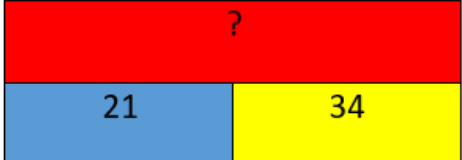
11

£	2	3	.	5	9
+	£	7	.	5	5
£	3	1	.	1	4
	1	1		1	

2	3	.	3	6	1
	9	.	0	8	0
5	9	.	7	7	0
+	1	.	3	0	0
9	3	.	5	1	1
2	1		2		

Fluency variation, different ways to ask children to solve $21 + 34$:

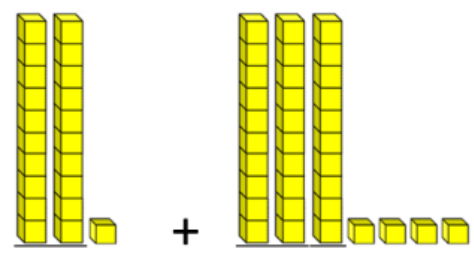







Sam saved £21 one week and £34 another. How much did he save in total?
 21+34=55. Prove it! (reasoning but the children need to be fluent in representing this)

$$\begin{array}{r} 21 \\ +34 \\ \hline \end{array}$$

21 + 34 =
 $\square = 21 + 34$
 What's the sum of twenty one and thirty four?



Always use missing digit problems too:

Tens	Ones
	
	?
?	4

Subtraction

Key Vocabulary – take away, less than, the difference, subtract, minus, fewer, decrease, ‘7 take away 3, the difference is four’

(Year group) Objective and Strategies	Concrete	Pictorial	Abstract
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(Year 1)
Taking away
ones

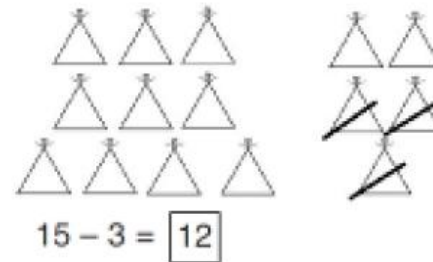
Use physical objects, counters, cubes etc to show how objects can be taken away. Rather than crossing out, the children will physically remove the objects.

$$4 - 3 = 1$$



$$4 - 2 = 2$$

Cross out drawn objects to show what has been taken away.



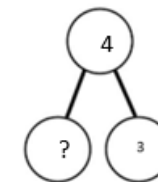
Use of the bar model



$$8 - 2 =$$

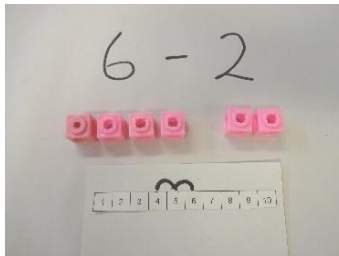
$$\square = 8 - 2$$

4	
3	?



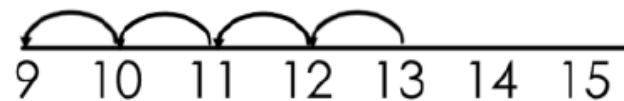
(Year 1)
Counting back

Count back using number lines or number tracks

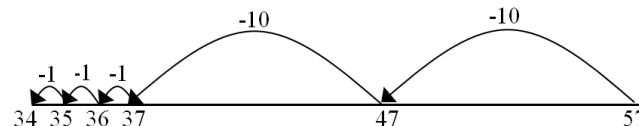


Make the larger number in your subtraction. Move the beads along your bead string as you count backwards in ones.

$$13 - 4$$

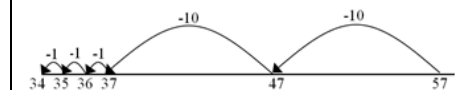
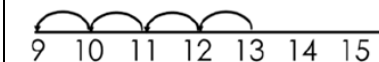
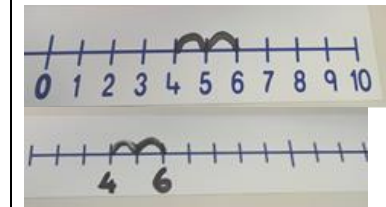


Start at the bigger number and count back the smaller number showing the jumps on the number line.



This can progress all the way to counting back using two 2 digit numbers.

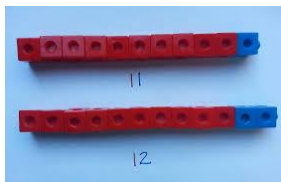
Count back on a number line or number track



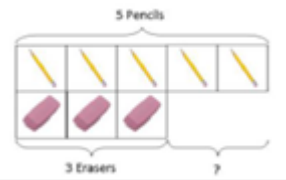
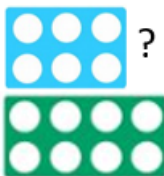
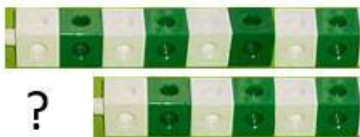
This can progress all the way to counting back using two 2 digit numbers. (Year 2)

(Year 1) Find the difference

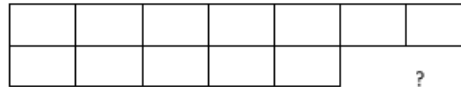
Compare amounts and objects to find the difference. Use cubes, numicon, and other objects.



Use cubes to build towers or make bars to find the difference



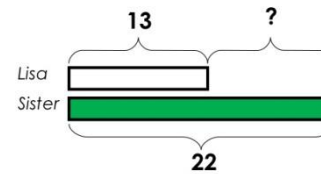
Use basic bar models with items to find the difference



Comparison Bar Models

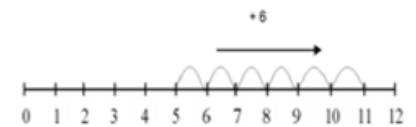
Draw bars to find the difference between 2 numbers.

Lisa is 13 years old. Her sister is 22 years old. Find the difference in age between them.



Children to draw the cubes/other concrete objects which they have used

XXXXXXXXX
XXXXXX



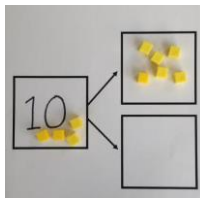
Count on to find the difference.

Hannah has 23 sandwiches, Helen has 15 sandwiches. Find the difference between the number of sandwiches.

Find the difference between 8 and 6.

8 - 6, the difference is ?
Children to also explore why 9 - 7 = 8 - 6 (the difference, of each digit, has changed by 1 do the difference is the same- this will help when solving 10000-9987)

Part Part Whole Model

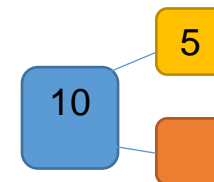
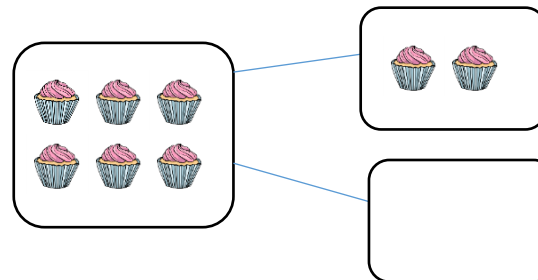


Link to addition- use the part whole model to help explain the inverse between addition and subtraction.

If 10 is the whole and 6 is one of the parts. What is the other part?

$$10 - 6 =$$

Use a pictorial representation of objects to show the part part whole model.



Move to using numbers within the part whole model.

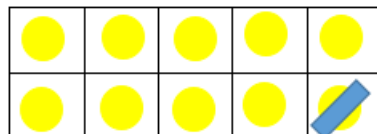
Make 10

Using numicon or 10 frames

$$14 - 5 =$$



Children to present the 10 frame pictorially.



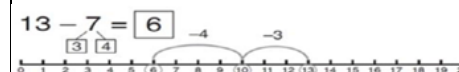
$14 - 5 = 9$ You also want children to see related facts e.g. $15 - 9 = 5$
Children to represent how they have solved it e.g.

$$\begin{array}{r} 14 - 5 = 9 \\ \swarrow \quad \searrow \\ 5 \quad 5 \end{array}$$

14 is made up of 5, 5 and 4 so I can subtract one 5 to be left with 4 and 5

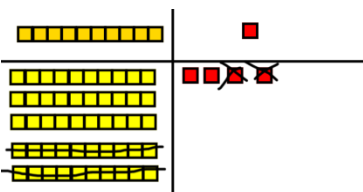
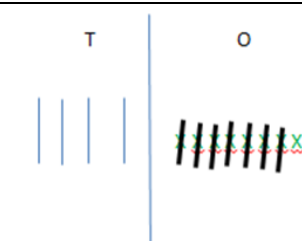
$$\begin{array}{r} 14 - 5 = 9 \\ \swarrow \quad \searrow \\ 4 \quad 1 \end{array}$$

5 is made up of 4 and 1 so I can subtract 4 to make 10 and then 1 to get to 9



Column method without regrouping

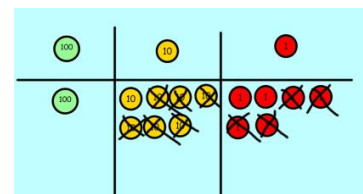
Use base 10 (2-digit - 1-digit, 2-digit - 2-digit and beyond)



Calculations

$$\begin{array}{r} 54 \\ - 22 \\ \hline 32 \end{array}$$

Draw the Base 10 or place value counters alongside the written calculation to help to show working.



Calculations

$$\begin{array}{r} 176 \\ - 64 \\ \hline 112 \end{array}$$

$$47 - 24 = 23$$

$$\begin{array}{r} 40 + 7 \\ - 20 + 4 \\ \hline 20 + 3 \end{array}$$

This will lead to a clear written column subtraction

Column method with regrouping

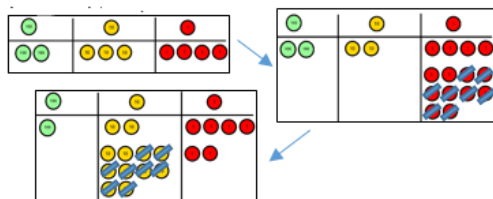
Using Base 10 and having to exchange.

45-26

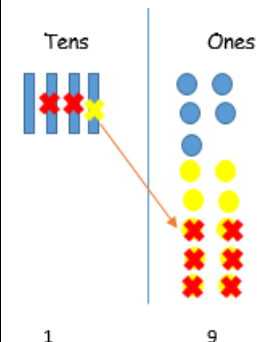


- 1) Start by partitioning 45
- 2) Exchange one ten for ten more ones
- 3) Subtract the ones, then the tens.

Using place value counters
234-88



Represent the base 10 pictorially



Once the children have had practice with the concrete, they should be able to apply it to any subtraction.

Like the other pictorial representations, children to represent the counters.

$$\begin{array}{r} 836 - 254 = 582 \\ \begin{array}{c} \text{H} \quad \text{T} \quad \text{U} \\ 800 \quad 130 \quad 6 \\ - 200 \quad 50 \quad 4 \\ \hline 500 \quad 80 \quad 2 \end{array} \end{array}$$

Children can start their formal written method by partitioning the number into clear place value columns.

$$\begin{array}{r} 728 - 582 = 146 \\ \begin{array}{c} \text{H} \quad \text{T} \quad \text{U} \\ 700 \quad 20 \quad 8 \\ - 500 \quad 80 \quad 2 \\ \hline 100 \quad 40 \quad 6 \end{array} \end{array}$$

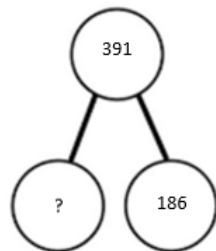
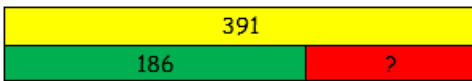


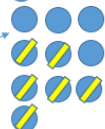


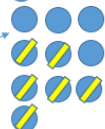


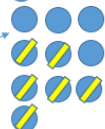
It's crucial that the children understand that when they have exchanged the 10 they still have 45. $45 = 30 + 15$

$$\begin{array}{r} 45 \\ - 26 \\ \hline 19 \end{array}$$

This will lead to an understanding of subtracting any number including decimals.

$$\begin{array}{r} 5 \quad 12 \quad 1 \\ 2 \quad 6 \quad 3 \quad . \quad 0 \\ - 2 \quad 6 \quad . \quad 5 \\ \hline 2 \quad 3 \quad 6 \quad . \quad 5 \end{array}$$

Fluency variation, different ways to ask children to solve 391-186

 	<p>Raj spent £391, Timmy spent £186. How much more did Raj spend?</p> <p>I had 391 metres to run. After 186 I stopped. How many metres do I have left to run?</p>	<p>391 - 186</p> <p><input type="text"/> = 391 - 186</p> <p>391 <u>-186</u></p> <p>Find the difference between 391 and 186</p> <p>Subtract 186 from 391.</p> <p>What is 186 less than 391?</p>	<p>What's the calculation? What's the answer?</p> <table border="1" data-bbox="1621 341 2085 549"><thead><tr><th>Hundreds</th><th>Tens</th><th>Ones</th></tr></thead><tbody><tr><td></td><td></td><td></td></tr></tbody></table> <table data-bbox="1632 604 1823 780"><tr><td></td><td>3</td><td>9</td><td><input type="text"/></td></tr><tr><td>-</td><td><input type="text"/></td><td><input type="text"/></td><td>6</td></tr><tr><td colspan="4"><hr/></td></tr><tr><td></td><td><input type="text"/></td><td>0</td><td>5</td></tr></table>	Hundreds	Tens	Ones					3	9	<input type="text"/>	-	<input type="text"/>	<input type="text"/>	6	<hr/>					<input type="text"/>	0	5
Hundreds	Tens	Ones																							
																									
	3	9	<input type="text"/>																						
-	<input type="text"/>	<input type="text"/>	6																						
<hr/>																									
	<input type="text"/>	0	5																						

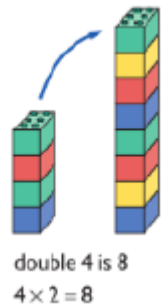
Multiplication

Key vocabulary- double, times, multiplied by, the product of, groups of, lots of, 'is equal to', 'is the same as'

Objective and Strategies	Concrete	Pictorial	Abstract
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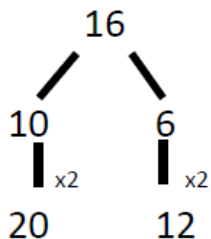
Doubling

Use practical activities to show how to double a number.



Draw pictures to show how to double a number.

Double 4 is 8

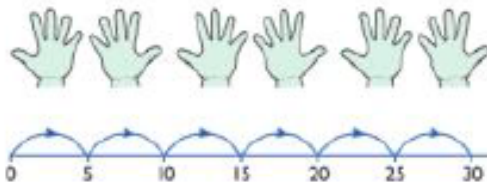


Partition a number and then double each part before recombining it back together.

Counting in multiples



Count in multiples supported by concrete objects in equal groups.



Use a number line or pictures to continue support in counting in multiples.

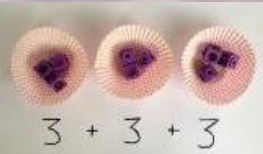
Count in multiples of a number aloud.

Write sequences with multiples of numbers.

2, 4, 6, 8, 10

5, 10, 15, 20, 25, 30

Repeated grouping/ addition

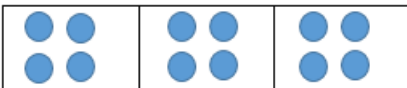


Use different objects to add equal groups.

Children to represent the practical resources in a picture, e.g.




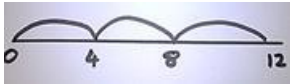

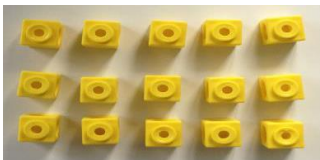
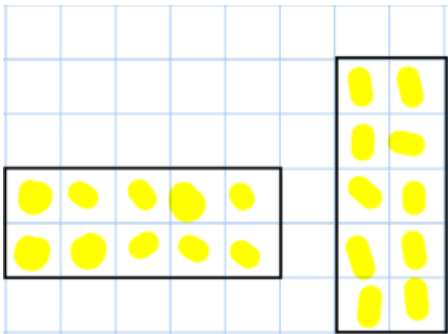

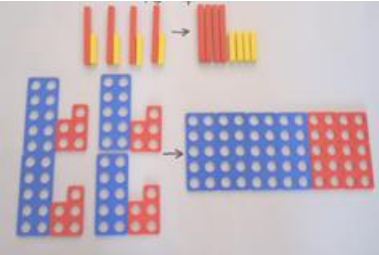
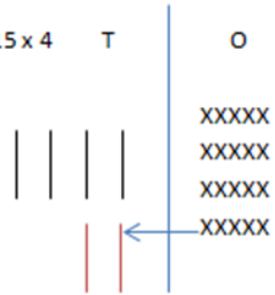
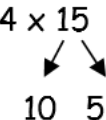
XX XX
XX XX
XX XX

Use of a bar model for a more structures method.



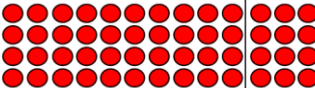

3×4

$4 + 4 + 4$

<p>Use number lines to show repeated groups</p>	<p>3 x 4</p>  	<p>Represent this pictorially alongside a number line, e.g.</p> 	<p>Abstract number line</p> 
<p>Arrays- showing commutative multiplication</p>	<p>Create arrays using counters/ cubes to show multiplication sentences.</p>  	<p>Children to draw the arrays.</p> 	<p>Use an array to write multiplication sentences and reinforce repeated addition.</p>  <p> $5 + 5 + 5 = 15$ $3 + 3 + 3 + 3 + 3 = 15$ $5 \times 3 = 15$ $3 \times 5 = 15$ </p>
<p>Partition to multiply</p>	<p>Use numicon or Base 10.</p> <p>4 x 15</p> 	<p>Children to represent the concrete manipulatives in a picture, e.g Base 10 can be represented like:</p> <p>15 x 4 T O</p> 	<p>Children to be encouraged to show the steps they have taken</p> <p>4 x 15</p>  <p> $10 \times 4 = 40$ $5 \times 4 = 20$ $40 + 20 = 60$ </p>



Grid Method

Show the link with arrays to first introduce the grid method.

x	10	3
4		




4 rows
of 10
4 rows
of 3

Move on to using Base 10 to move towards a more compact method.

x	T	U
		
















4 rows of 13

Move on to place value counters to show how we are finding groups of a number. We are multiplying by 4 so we need 4 rows.

Calculations
4 x 126

Fill each row with 126.

Calculations
4 x 126

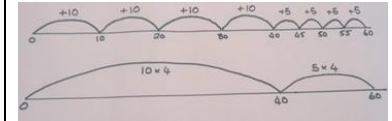
Add up each column, starting with the ones making any exchanges needed.

Children can represent the work they have done with place value counters in a way that they understand.

They can draw the counters, using colours to show different amounts or just use circles in the different columns to show their thinking as shown below.

	24	x	3	=	72
x	20		4		
3	00		0000		
	00		0000		
	00		0000		
	60		12		
			60		
			+ 12		
			72		

A number line can also be used



Start with multiplying by one digit numbers and showing the clear addition alongside the grid.

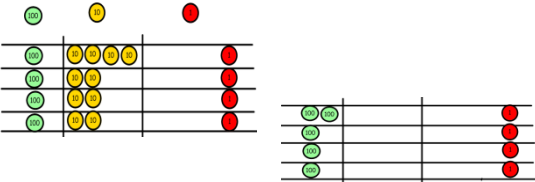

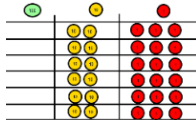
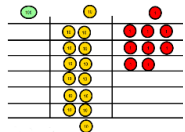
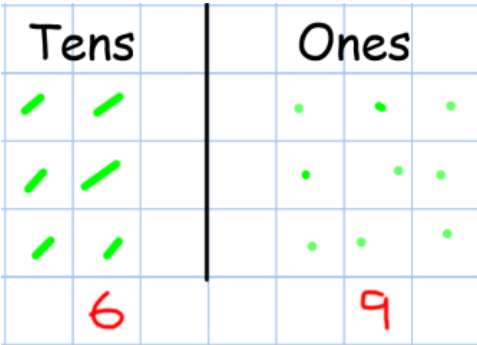
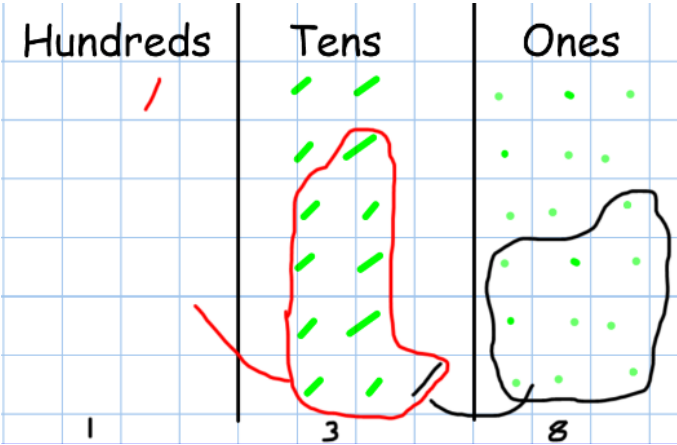
x	30	5
7	210	35

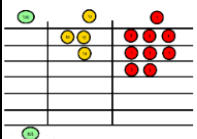
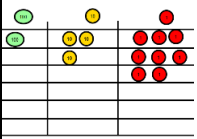
$$210 + 35 = 245$$

Moving forward, multiply by a 2 digit number showing the different rows within the grid method.

	10	8
10	100	80
3	30	24

x	1000	300	40	2
10	10000	3000	400	20
8	8000	2400	320	16

	 <p>Then you have your answer.</p>		
Column multiplication	<p>Use place value counters or base 10 (at the first stage – no exchanging) 3×23</p> <p>Make 23, 3 times. See how many ones, then how many tens.</p>  <p>6×23</p>  <p>Step 1: get 6 lots of 23</p>  <p>Step 2: 6×3 is 18. Can I make an exchange? Yes! Ten ones for one ten....</p>	<p>Children to represent the counters in a pictorial way</p>  	<p>Children to record what it is they are doing to show understanding</p> $ \begin{array}{r} 3 \times 23 \\ \hline 20 \quad 3 \end{array} $ $ \begin{array}{rcl} 3 \times 20 & = & 60 \\ 3 \times 3 & = & 9 \\ 60 + 9 & = & 69 \end{array} $ <p>The aim is to get to the formal method but the children need to understand how it works.</p> $6 \times 23 =$ $ \begin{array}{r} 23 \\ \times 6 \\ \hline 138 \\ \hline 1 \quad 1 \end{array} $

	 <p>Step 3: 6 x 2 tens and my extra ten is 13 tens. Can I make an exchange? Yes! Ten tens for one hundred...</p>		
	 <p>Step 4- what do I have in each column?</p>		

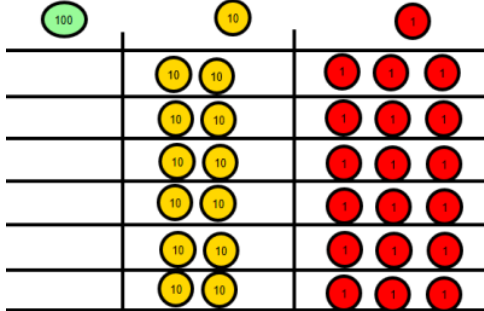
When children start to multiply 3d x 3d and 4d x 2d etc, they should be confident with the abstract:

To get 744 children have solved 6 x 124
 To get 2480 they have solved 20 x 124


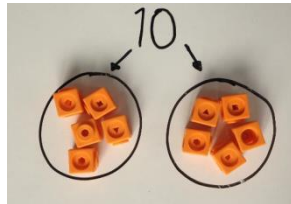
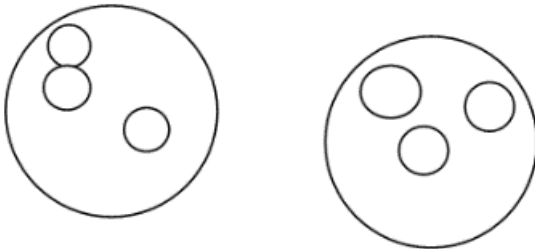
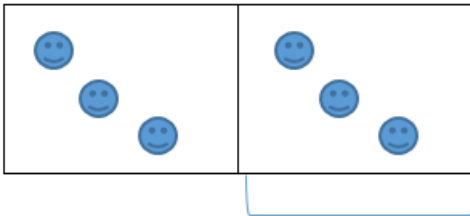
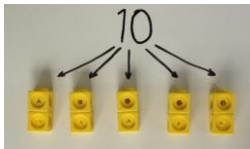
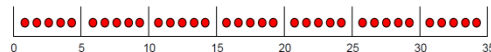


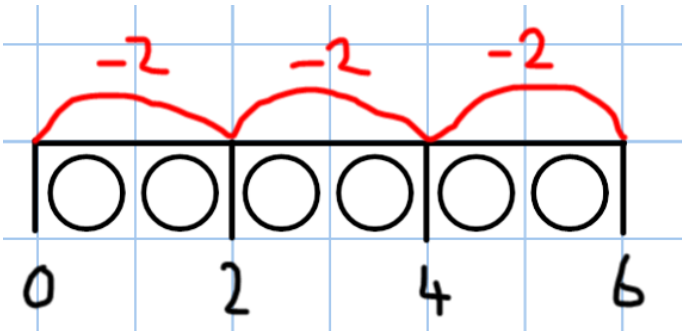
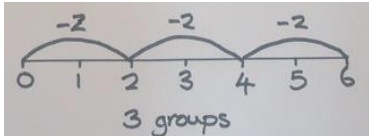
$$\begin{array}{r}
 1 \ 2 \ 4 \\
 \times \quad 2 \ 6 \\
 \hline
 7 \ 4 \ 4 \\
 \text{\tiny -1} \quad \text{\tiny 2} \\
 2 \ 4 \ 8 \ 0 \\
 \hline
 3 \ 2 \ 2 \ 4 \\
 \text{\tiny 1} \quad \text{\tiny 1}
 \end{array}$$

Answer: 3224

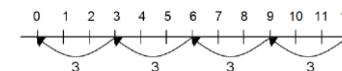
Fluency variation, different ways to ask children to solve 6 x 23

<div data-bbox="107 1018 477 1094"> <div>23</div><div>23</div><div>23</div><div>23</div><div>23</div><div>23</div> </div> <div data-bbox="293 1110 309 1133">?</div> <p>With the counters, prove that 6 x 23 = 138</p> <p>Why is 6 x 23 = 32 x 6?</p>	<p>Mai had to swim 23 lengths, 6 times a week. How many lengths did she swim in one week?</p> <p>Tom saved 23p three days a week. How much did he save in 2 weeks?</p>	<p>Find the product of 6 and 23</p> <p>6 x 23 =</p> <div data-bbox="1106 1161 1249 1203"> <div></div>= 6 x 23 </div> <div data-bbox="1115 1233 1366 1406"> <div>623</div><div>236</div> <div><div>×</div><div>23</div></div><div><div>×</div><div>6</div></div> <div><div>—</div></div><div><div>—</div></div> </div>	<p>What's the calculation? What's the answer?</p> 
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Key vocabulary – share, group, divide, divided by, half, ‘is equal to’, ‘is the same as’

Objective and Strategies	Concrete	Pictorial	Abstract		
Sharing objects into groups	<div></div> <div><p>I have 10 cubes, can you share them equally in 2 groups?</p></div>	<div></div> <p>This can also be done in a bar so all 4 operations have a similar structure:</p> <div></div>	<div>$6 \div 2 = 3$<p>What's the calculation?</p><table><tr><td>3</td><td>3</td></tr></table></div>	3	3
3	3				
Division as grouping/ repeated subtraction	<p>Divide quantities into equal groups. Use cubes, counters, objects or place value counters to aid understanding.</p> <div></div> <div></div> <div></div>	<p>Children to draw a picture of objects grouped.</p> <div></div> <p>$6 \div 2 =$</p> <div></div>	<div>$28 \div 7 = 4$<p>Divide 28 into 7 groups. How many are in each group?</p><p>Use a number line to show jumps in groups. The number of jumps equals the number of groups.</p><div></div></div>		

$$96 \div 3 = 32$$



Think of the bar as a whole. Split it into the number of groups you are dividing by and work out how many would be within each group.



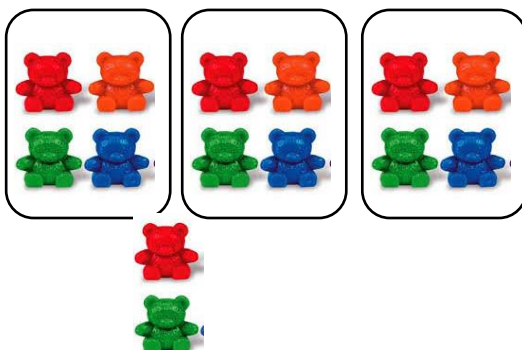
$$20 \div 5 = ?$$

$$5 \times ? = 20$$

Division with a remainder

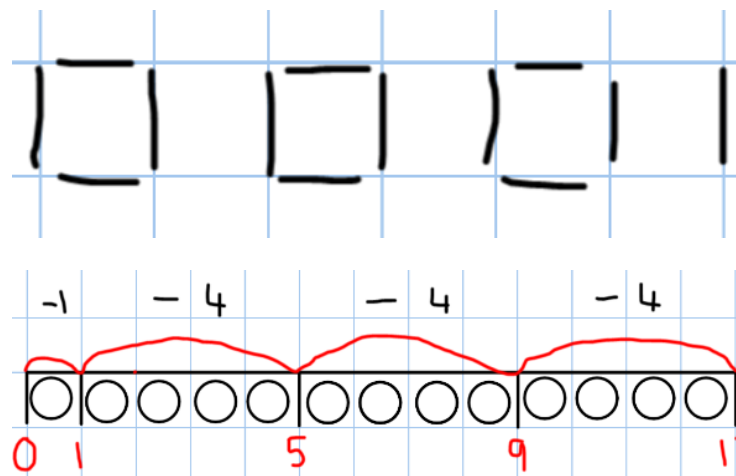
2d ÷ 1d

$14 \div 3 =$
Divide objects between groups and see how much is left over



Use of lolly sticks to form wholes

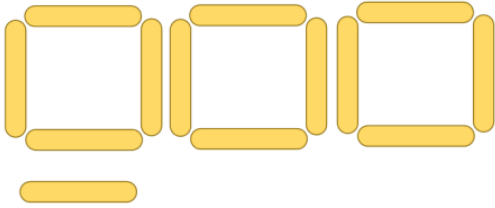
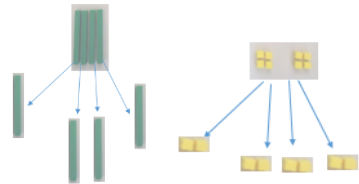
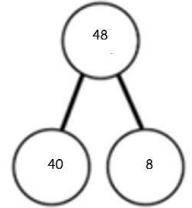
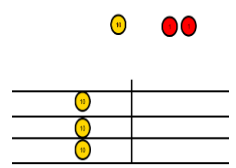
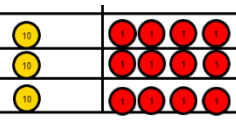
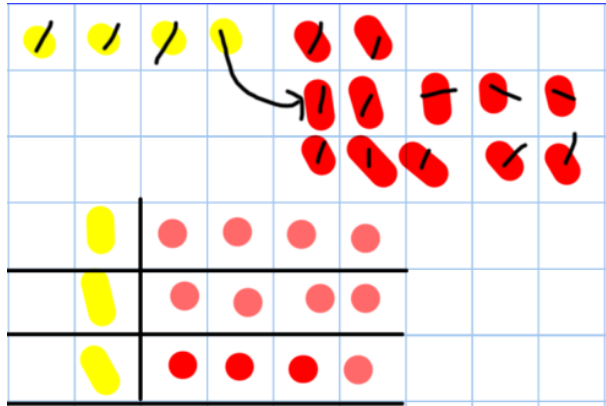
Children to represent the resources they use in a pictorial way.



Jump forward in equal jumps on a number line then see how many more you need to jump to find a remainder.

$$13 \div 4 = 3 \text{ r } 1$$



	 <p>$13 \div 4 =$</p>		
<p>Division using base 10 2d÷1d (no remainders) SHARING</p>	<p>$48 \div 4 = 12$</p>  <p>Start with the tens.</p>	<p>Children to represent the base 10 and sharing pictorially.</p>	<p>$48 \div 4$</p>  <p> $4 \text{ tens} \div 4 = 1 \text{ ten}$ $8 \text{ ones} \div 4 = 2 \text{ ones}$ $10 + 2 = 12$ </p>
<p>Sharing with place value counters</p>	<p>$42 \div 3 = 14$</p>  <p>1. Make 42. Share the 4 tens between 3. Can we make an exchange with the extra 10?</p>  <p>Exchange the ten for 10 ones and share out 12 ones</p>		<p>$42 \div 3$</p> <p>$42 = 30 + 12$</p> <p>$30 \div 3 = 10$</p> <p>$12 \div 3 = 4$</p> <p>$10 + 4 = 14$</p>

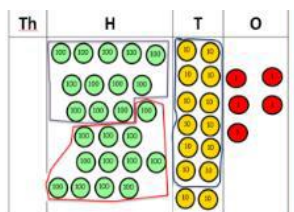
<p>'Bus stop' method</p>	<p>Use grouping and counters. Key language for grouping- how many groups of X can we make with X hundreds'- this can also be done using sharing!</p> <p>$615 \div 5$</p> <div data-bbox="409 379 651 528"> </div> <p>Step 1: make 615</p> <div data-bbox="409 536 651 684"> </div> <p>Step 2: Circle your groups of 5</p> <div data-bbox="409 692 651 841"> </div> <p>Step 3: Exchange 1H for 10T and circle groups of 5</p> <div data-bbox="409 865 651 1013"> </div> <p>Step 4: exchange 1T for 10ones and circles groups of 5</p>	<p>This can easily be represented pictorially, till the children no longer to do it. It can also be done to decimal places if you have a remainder!</p>	<p>Begin with divisions that divide equally with no remainder.</p> $\begin{array}{r} 218 \\ 4 \overline{) 872} \end{array}$ <p>Move onto divisions with a remainder.</p> $\begin{array}{r} 86 \text{ r } 2 \\ 5 \overline{) 432} \end{array}$ <p>Finally move into decimal places to divide the total accurately.</p> $\begin{array}{r} 123.0 \\ 35 \overline{) 511.0} \end{array}$
<p>Fluency variation, different ways to ask children to ask to solve $615 \div 5$</p>			
<p>Using the part whole model below, how can you divide 615 by 5 without using the 'bus stop' method?</p>	<p>I have £615 and share it equally between 5 bank accounts. How much will be in each account? 615 pupils need to be put into 5 groups. How many will be in each</p>	<p>$5 \overline{) 615}$</p> <p>$615 \div 5 =$</p>	<p>What's the calculation? What's the answer?</p>

<pre>graph TD; 615((615)) --- 500((500)); 615 --- 100((100)); 500 --- 15((15)); 100 --- 15</pre>	group?	<div><div></div> = 615 ÷ 5</div> <div>How many 5's go into 615?</div>	<table><tr><th>H</th><th>T</th><th>O</th></tr><tr><td></td><td></td><td></td></tr></table>	H	T	O			
H	T	O							

Long division

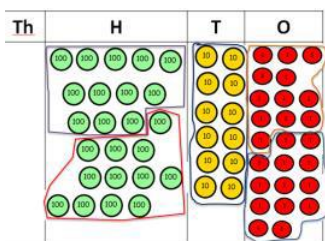
Concrete	Pictorial	Abstract																
<div><div><div>Model</div><table><tr><th>Th</th><th>H</th><th>T</th><th>O</th></tr><tr><td></td><td></td><td></td><td></td></tr></table></div><div><div>0 2 1 2</div><div>12 2544</div><div>24</div><div>14</div><div>12</div><div>24</div><div>24</div><div>0</div></div></div> <div><div>2544 ÷ 12</div><div>How many groups of 12 thousands do we have? None</div></div>	Th	H	T	O					<div>Children to represent the counters, pictorially and record the subtractions beneath.</div>	<div><div><div>0</div><div>12 2544</div></div><div>Step one- exchange 2 thousand for 20 hundreds so we now have 25 hundreds.</div></div> <div><div><div>0 2</div><div>12 2544</div><div>24</div><div>1</div></div><div>Step two- How many groups of 12 can I make with 25 hundreds? The 24 shows the hundreds we have grouped. The one is how many hundreds we have left.</div></div> <div><div><div>0 2 1</div><div>12 2544</div><div>24</div><div>14</div><div>12</div><div>2</div></div><div>Exchange the one hundred for 10 tens. How many groups of 12 can I make with 14 tens? The 14 shows how many tens I have, the 12 is how many I grouped and the 2 is how many tens I have left.</div></div>								
Th	H	T	O															
<div><div><div>Model</div><table><tr><th>Th</th><th>H</th><th>T</th><th>O</th></tr><tr><td></td><td></td><td></td><td></td></tr></table></div><div>Exchange 2 thousand for 20 hundreds.</div></div> <div><div><div>Model</div><table><tr><th>Th</th><th>H</th><th>T</th><th>O</th></tr><tr><td></td><td></td><td></td><td></td></tr></table></div><div><div>0 2</div><div>12 2544</div><div>24</div><div>1</div></div></div> <div><div>How many groups of 12 are in 25 hundreds? 2 groups. Circle them.</div></div>	Th	H	T	O					Th	H	T	O						
Th	H	T	O															
Th	H	T	O															

We have grouped 24 hundreds so can take them off and we are left with one.



$$\begin{array}{r} 021 \\ 12 \overline{) 2544} \\ \underline{24} \\ 14 \\ \underline{12} \\ 2 \end{array}$$

Exchange the one hundred for ten tens so now we have 14 tens. How many groups of 12 are in 14? 1 remainder 2.



Exchange the two tens for twenty ones so now we have 24 ones. How many groups of 12 are in 24? 2

$$\begin{array}{r} 0212 \\ 12 \overline{) 2544} \\ \underline{24} \\ 14 \\ \underline{12} \\ 24 \\ \underline{24} \\ 0 \end{array}$$

Exchange the 2 tens for 20 ones. The 24 is how many ones I have grouped and the 0 is what I have left.